

A large school of fish, likely salmon, swimming in clear blue water. The fish are densely packed and moving in various directions, creating a dynamic and textured background. The lighting is bright, highlighting the silvery scales of the fish.

# Poisson Regression

PSY504 Spring 2023



















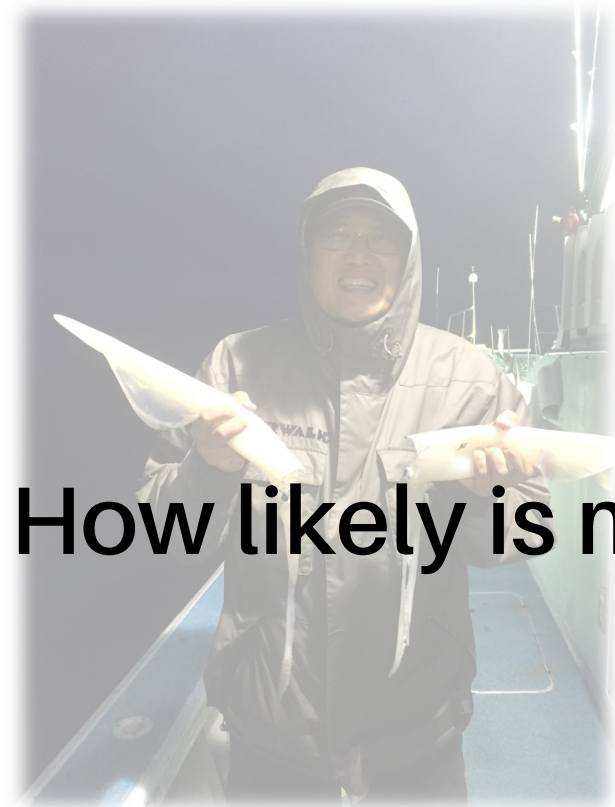










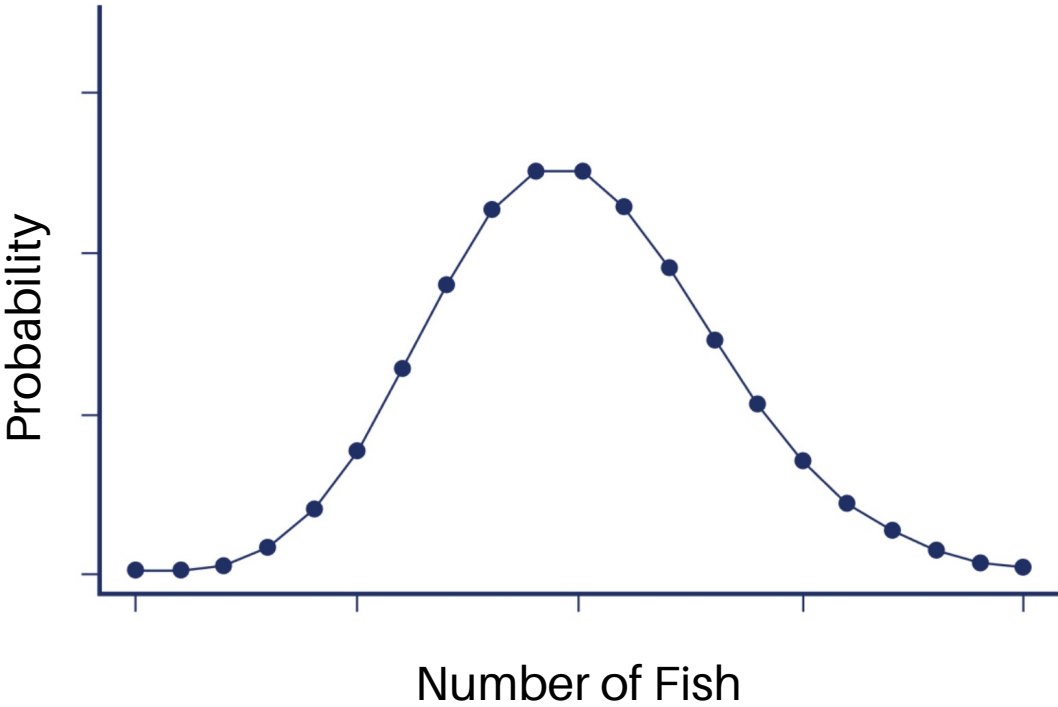


How likely is my dad to catch [#] of fish on any one trip?



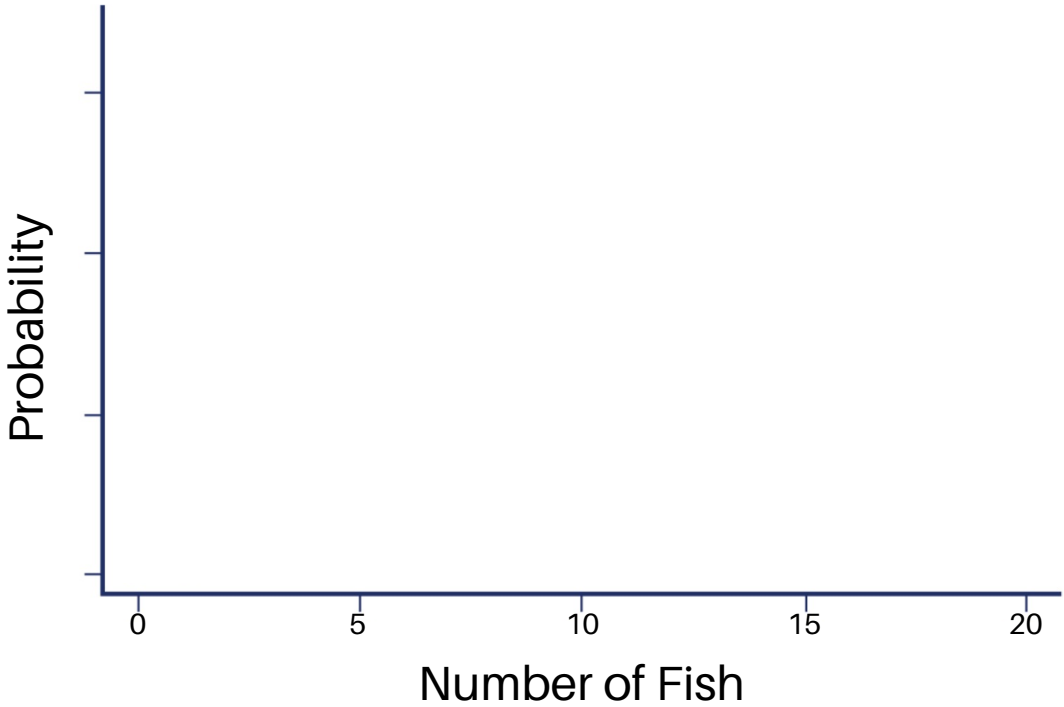
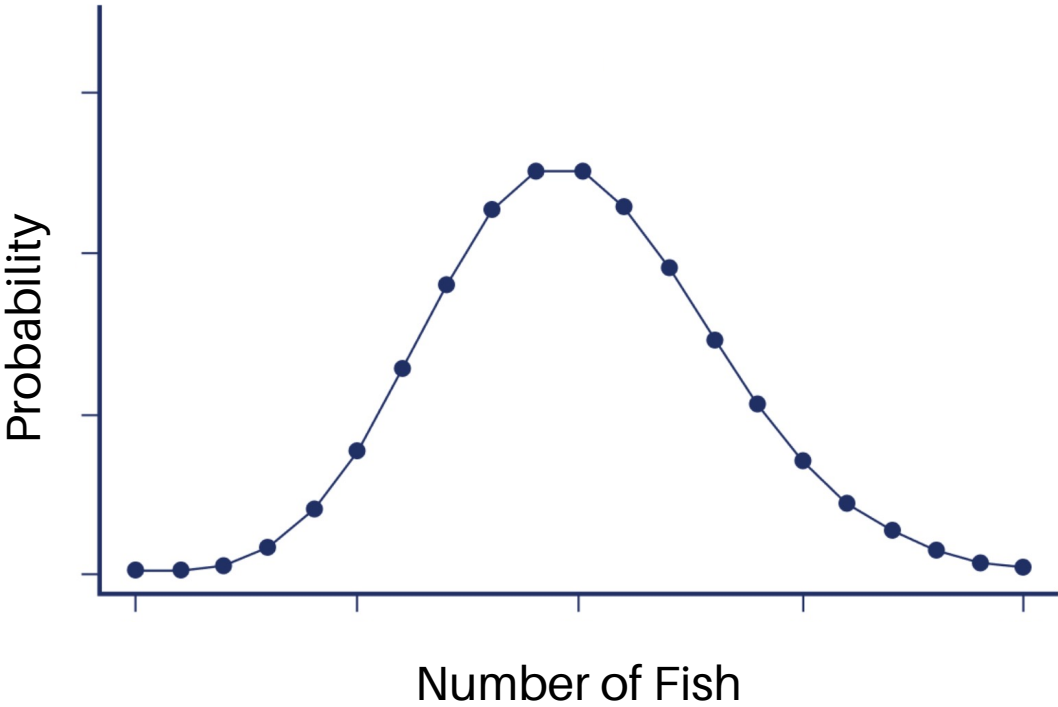
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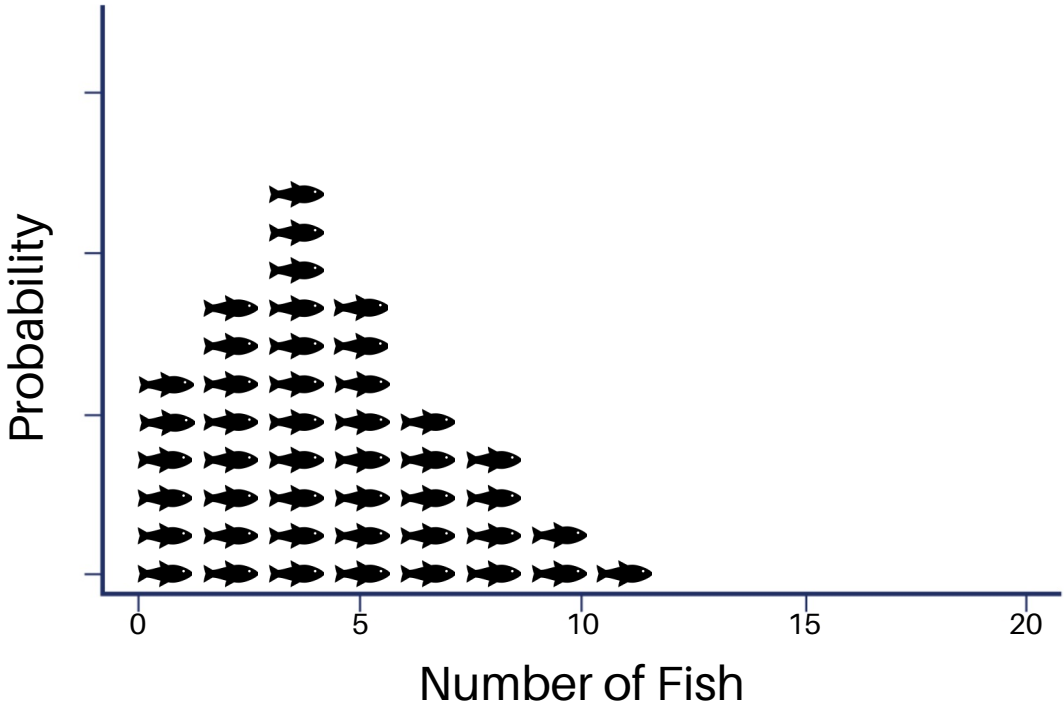
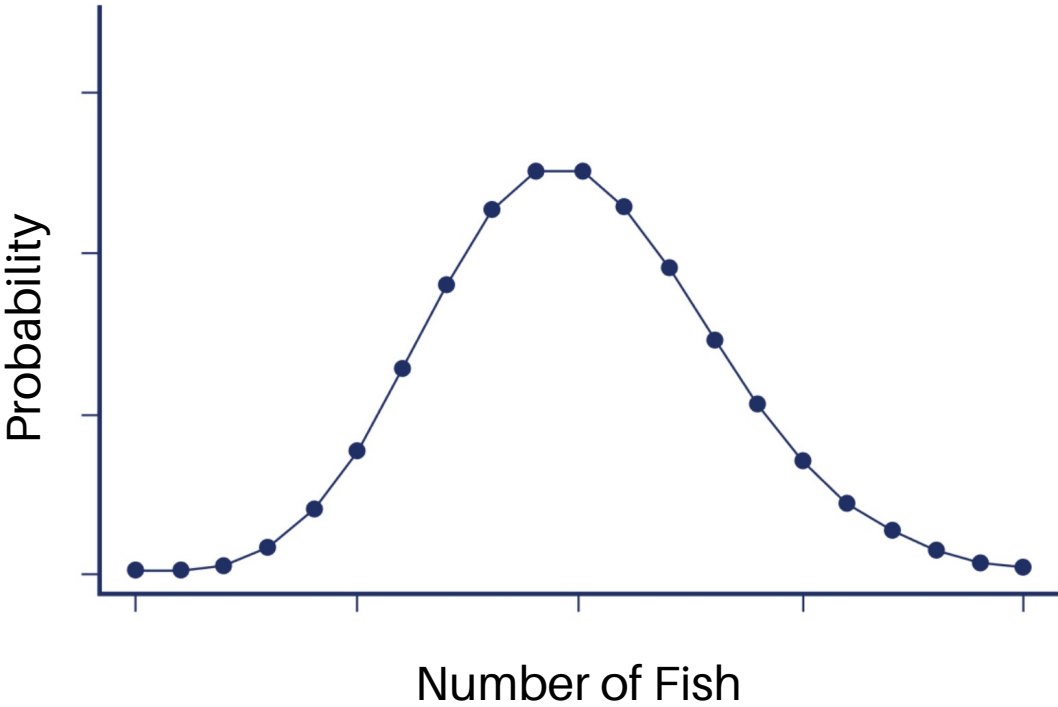




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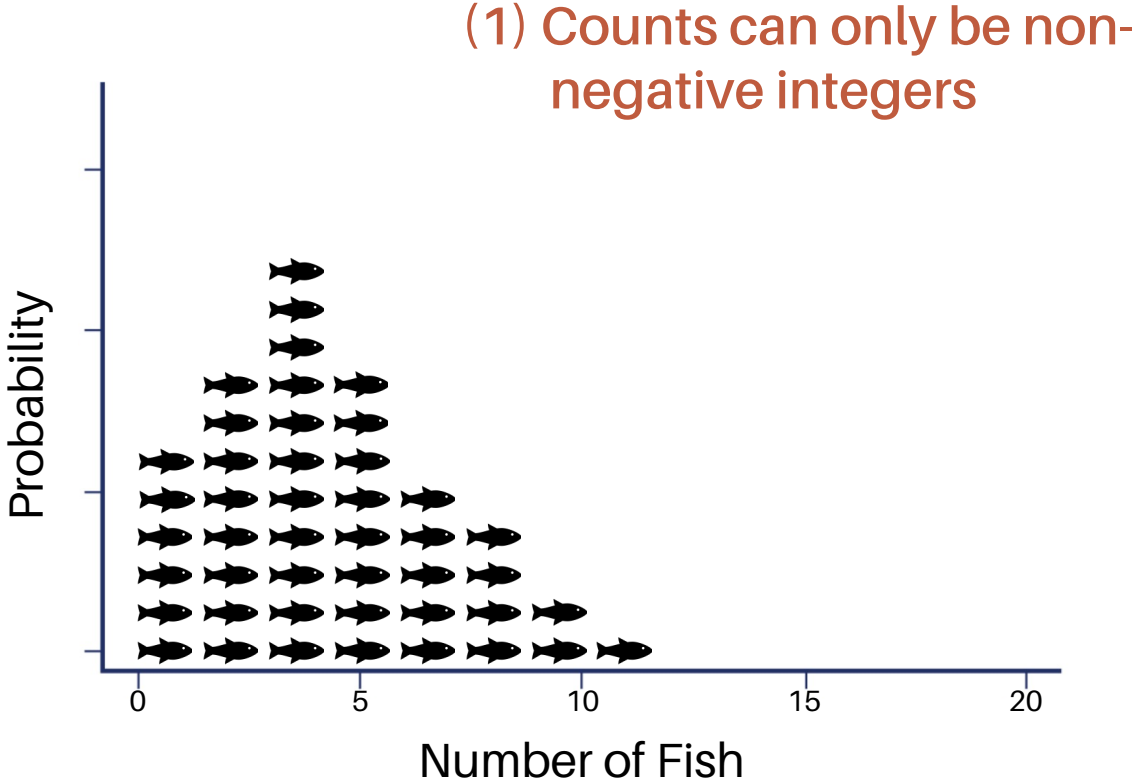
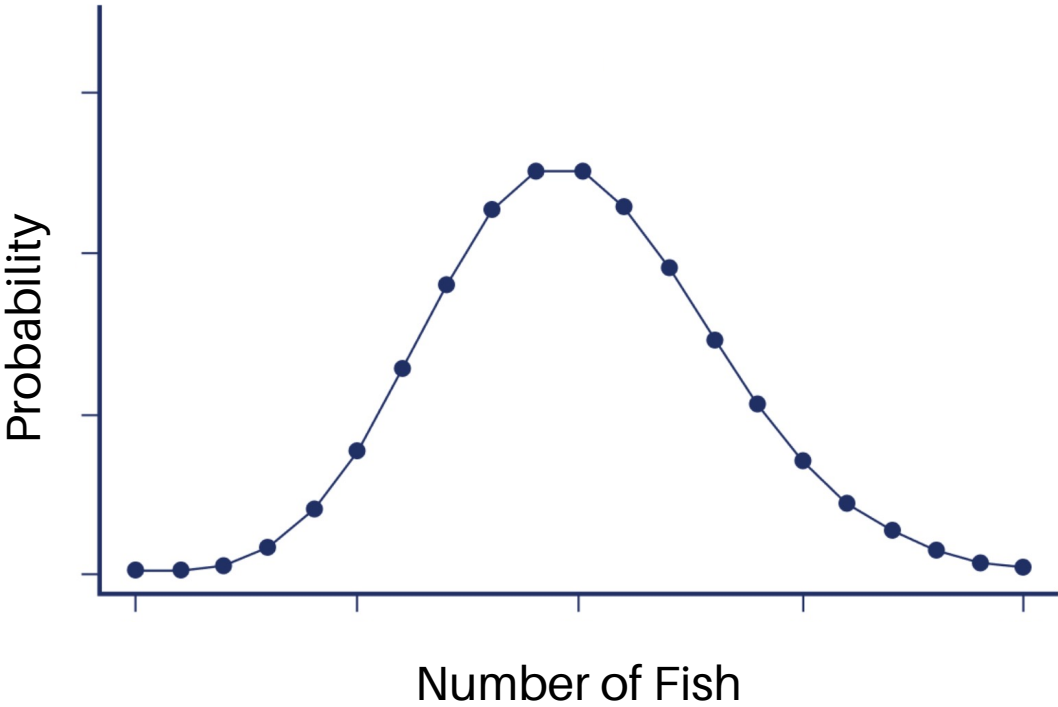


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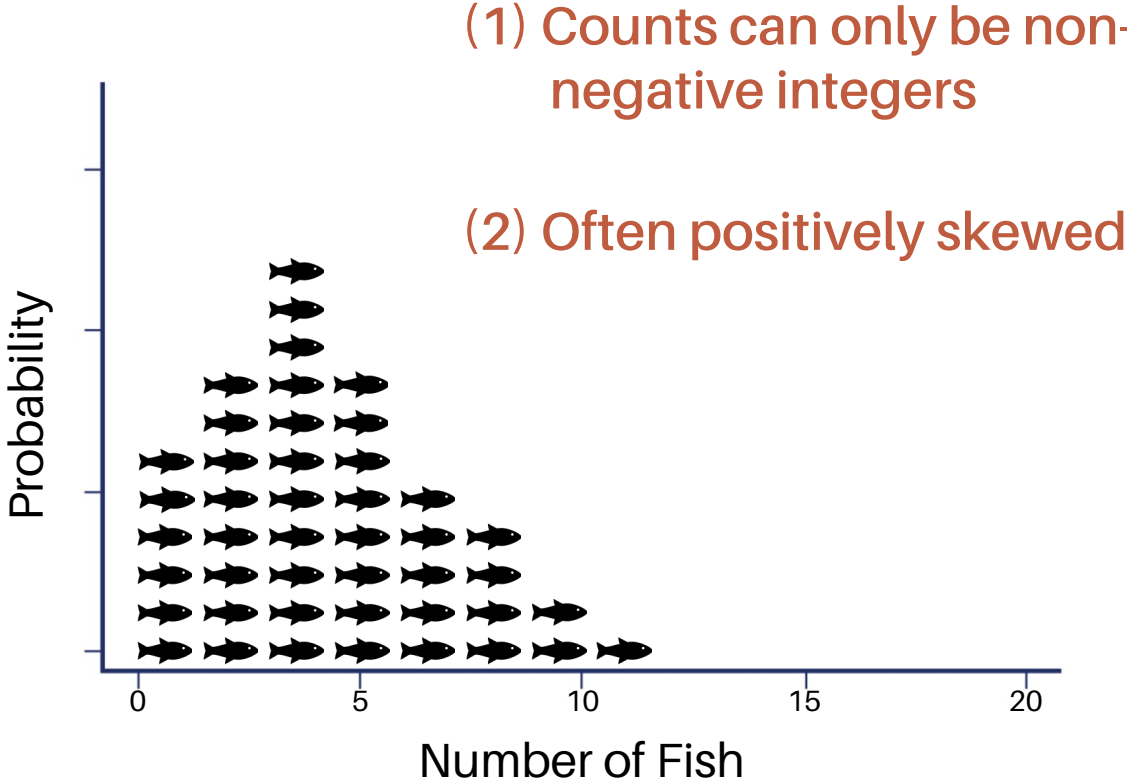
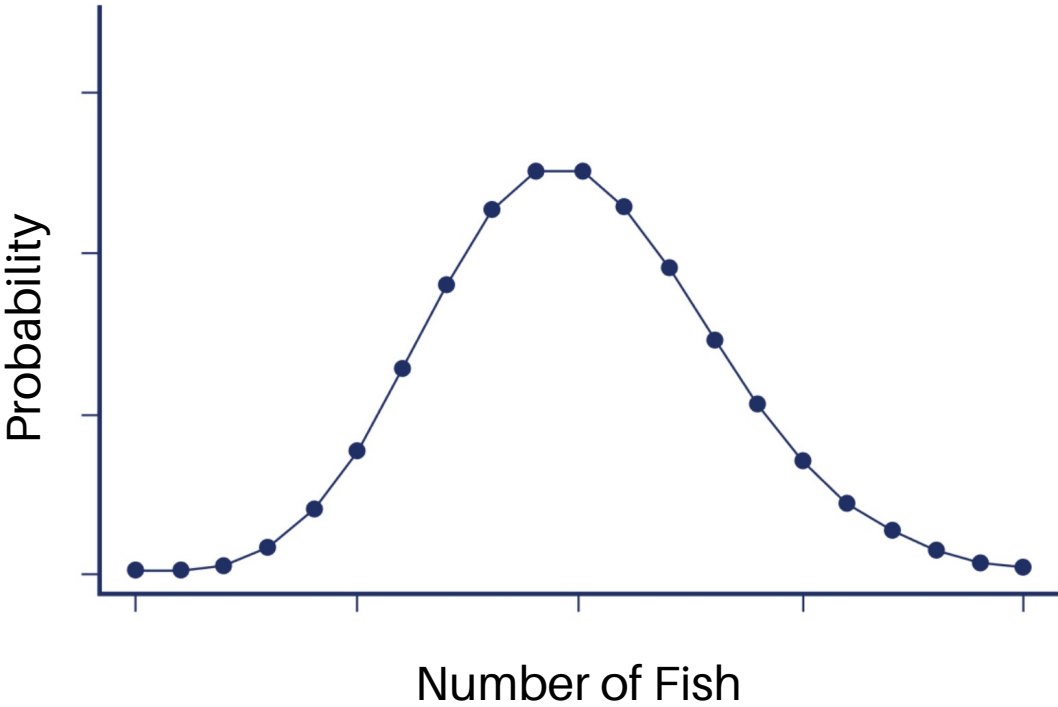




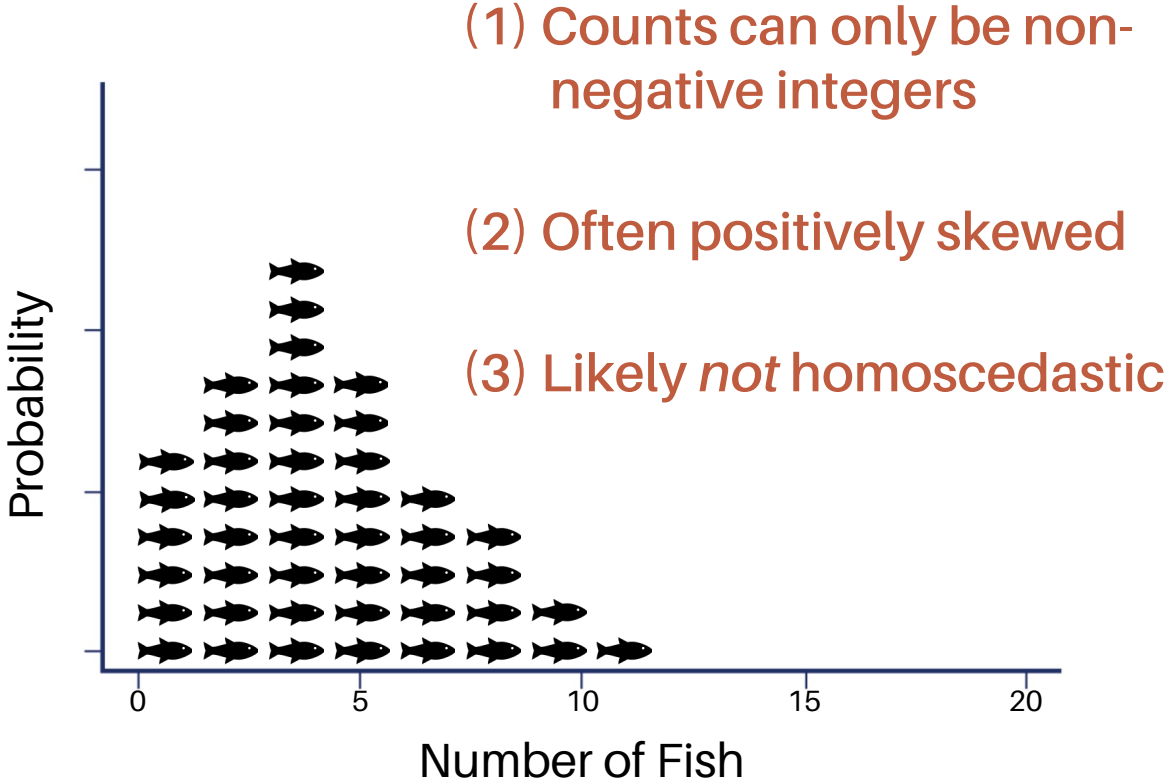
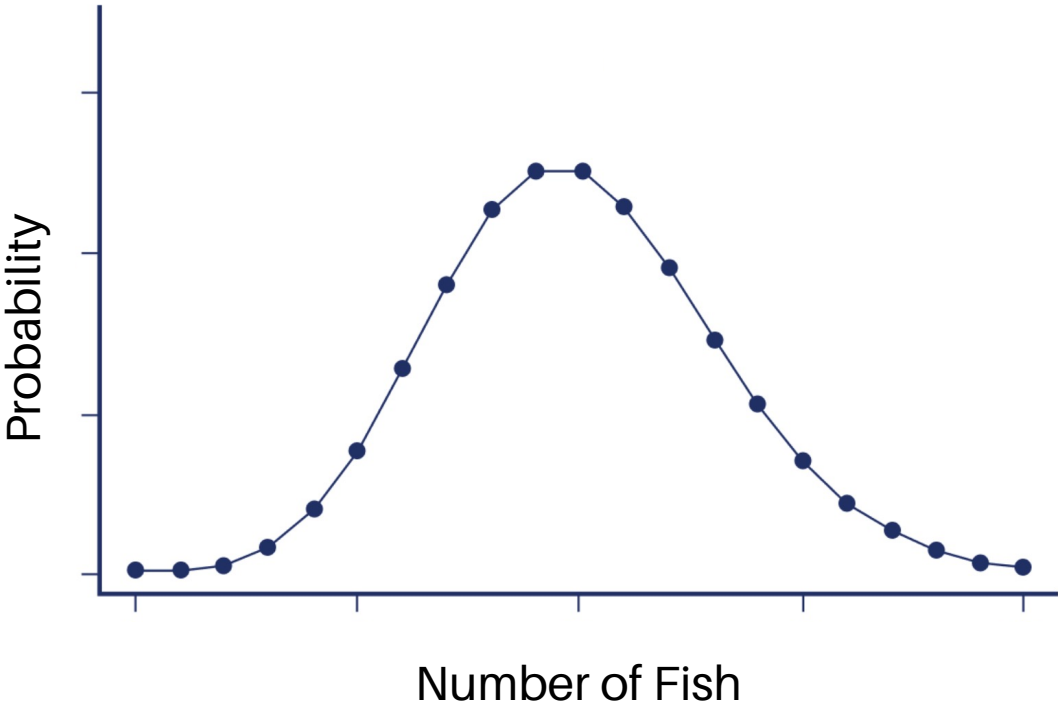
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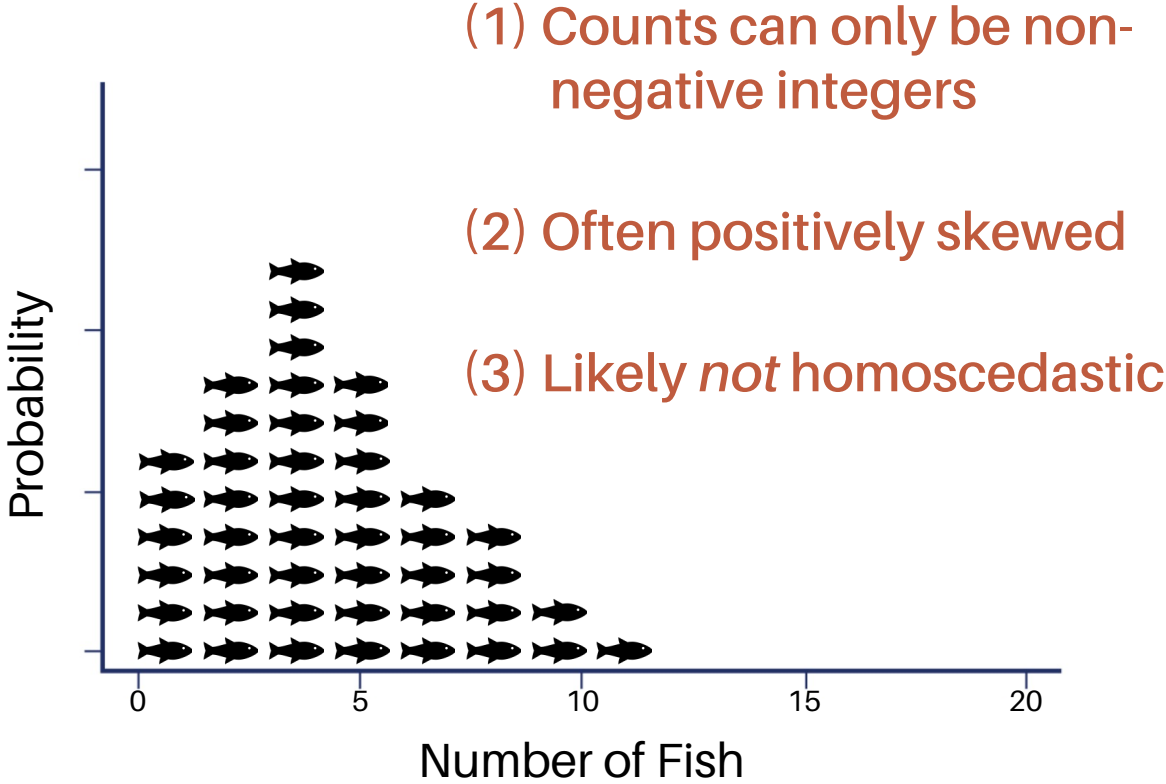
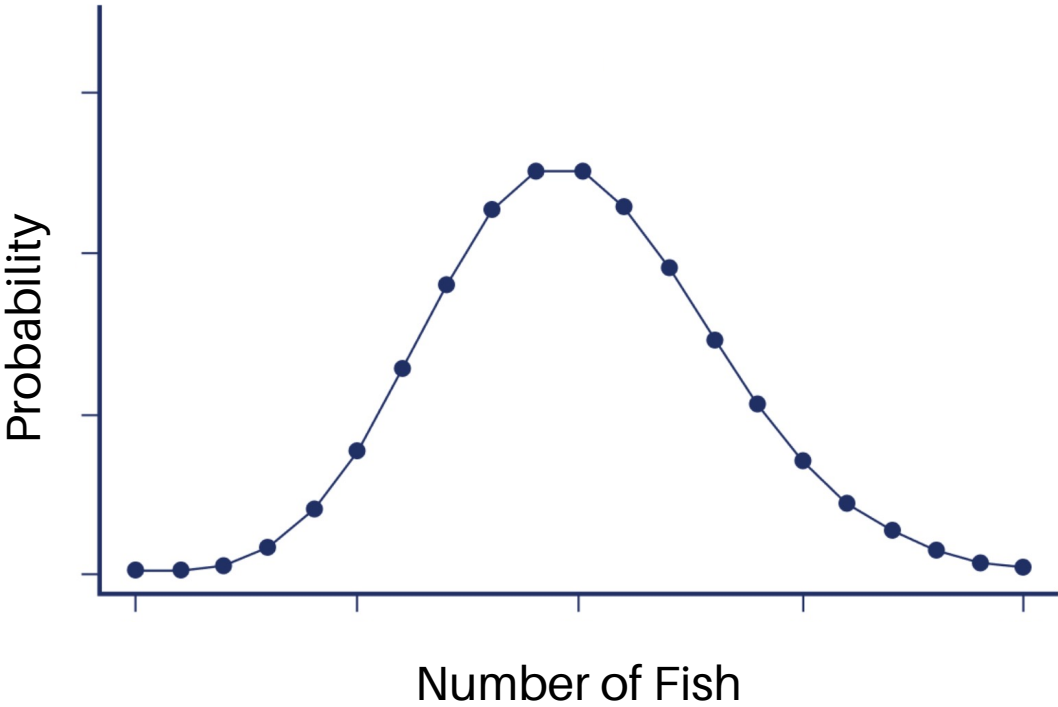


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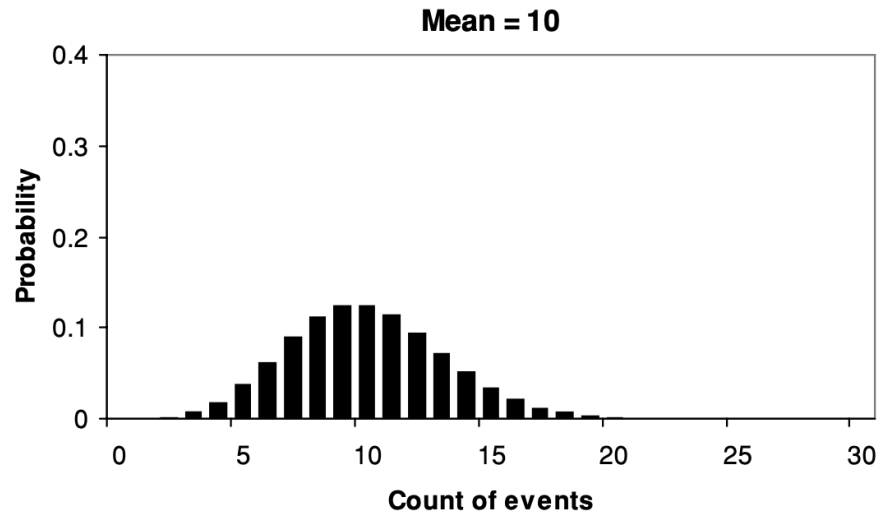
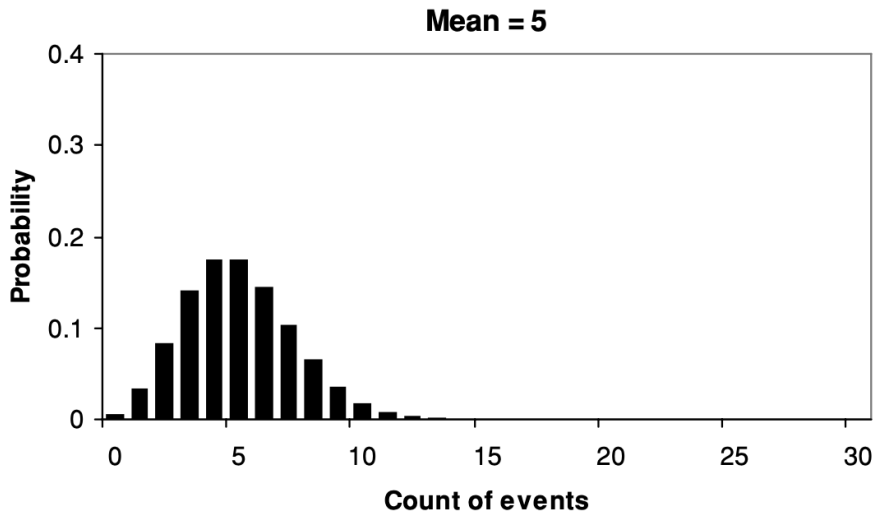
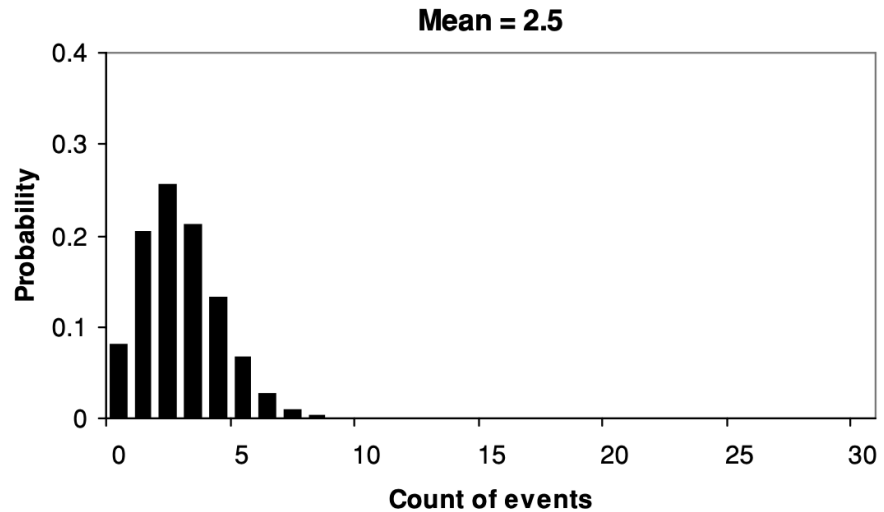
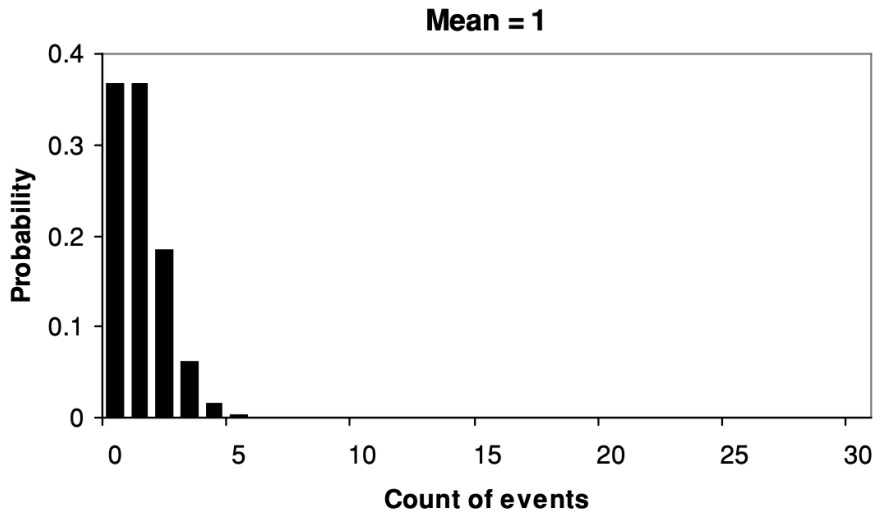


As a general rule, if the mean  $> 10$ , the poisson distribution approaches a normal distribution.

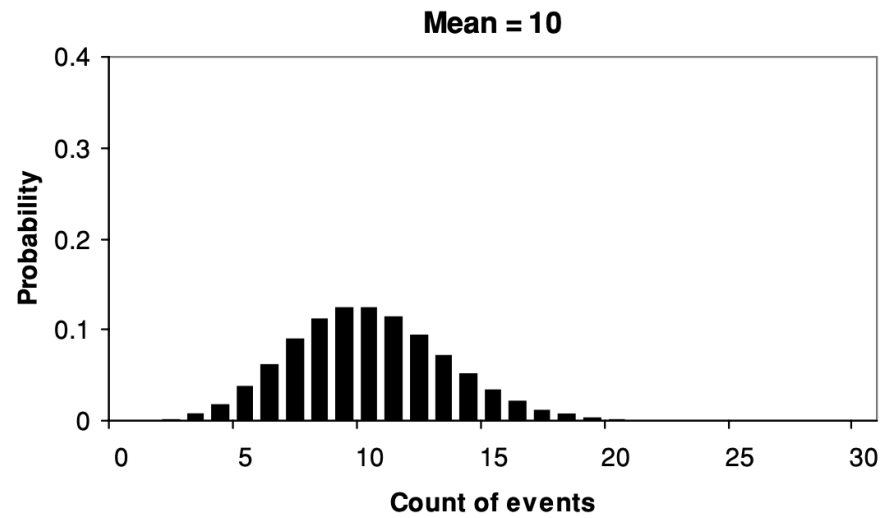
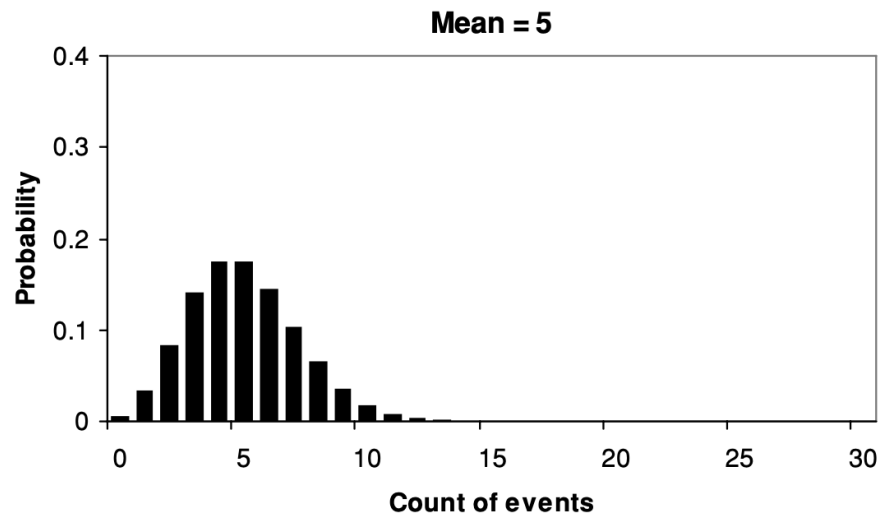
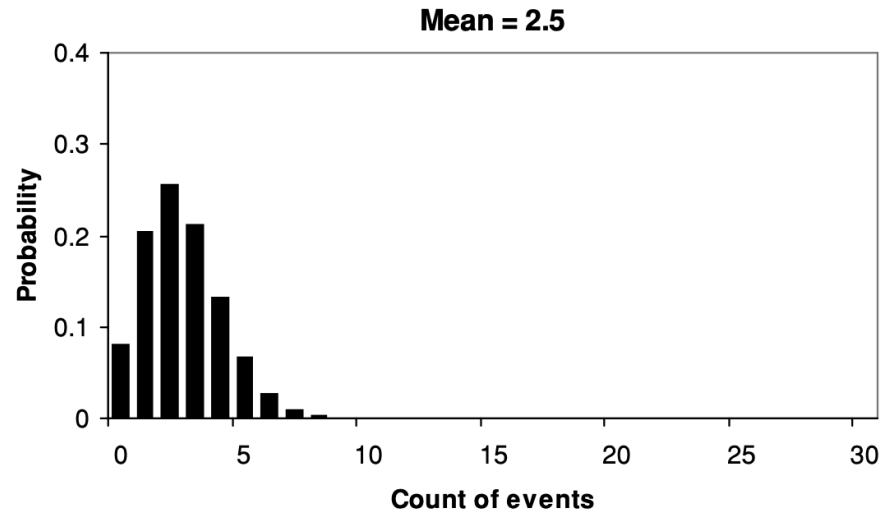
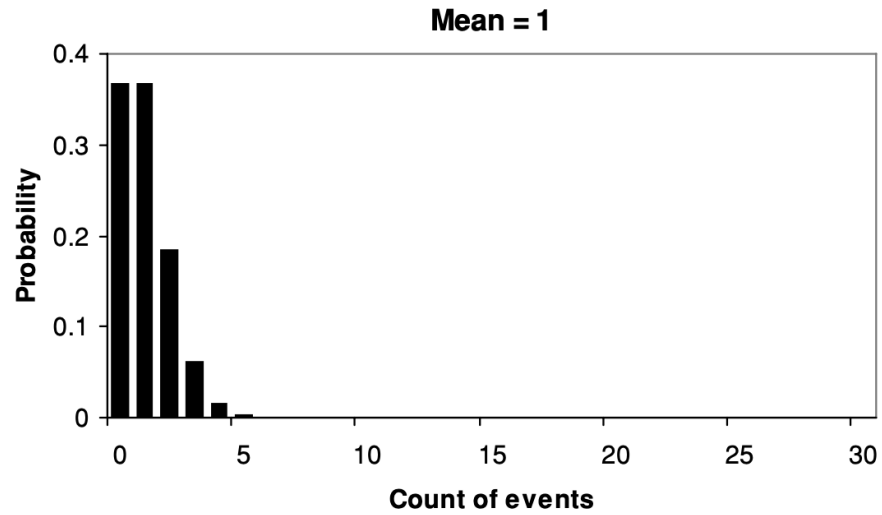
# Poisson distributions



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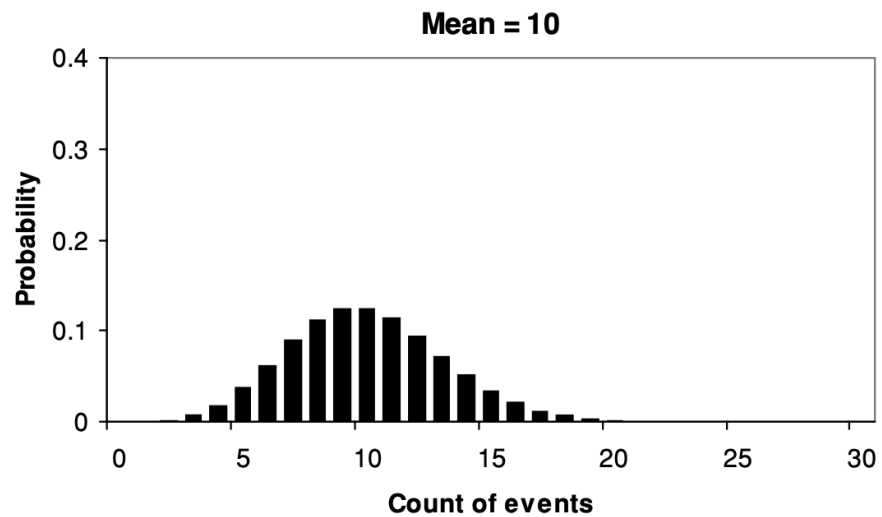
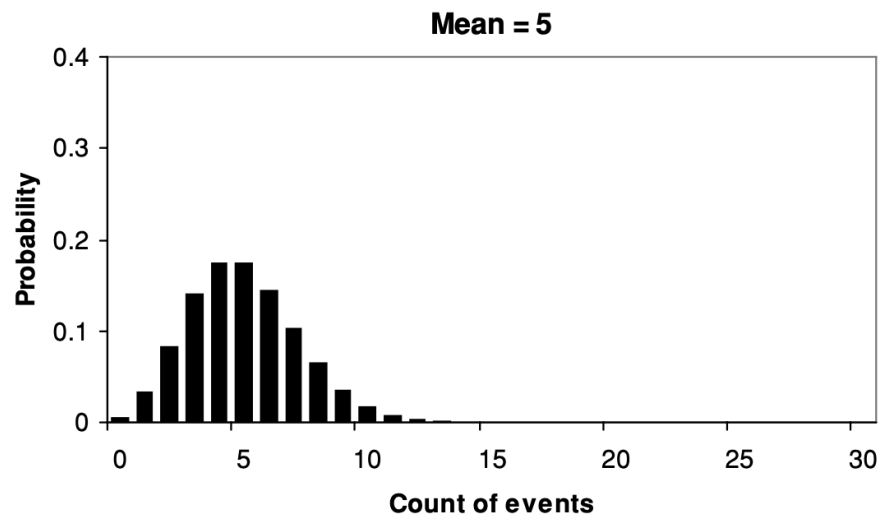
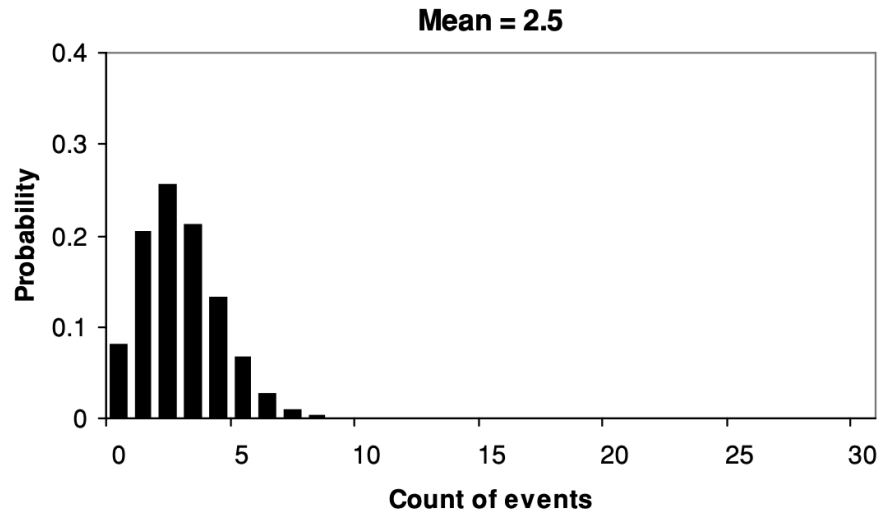
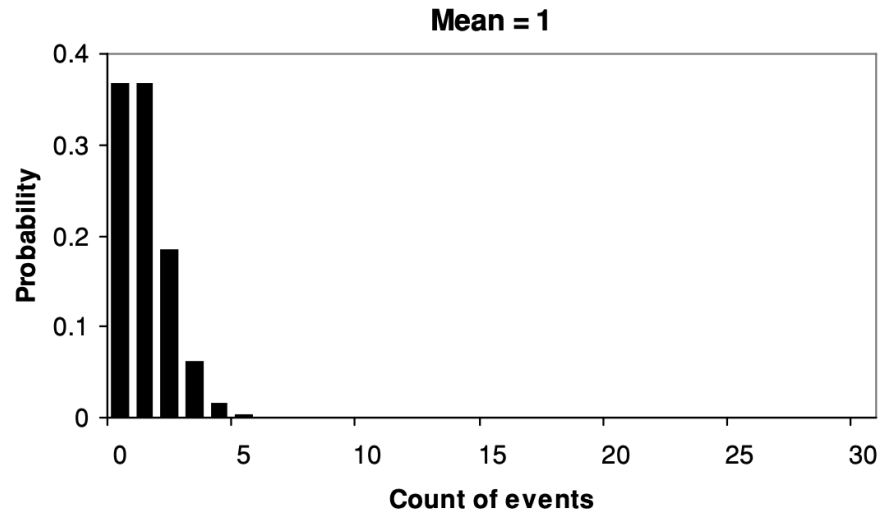


# Poisson distributions



One parameter,  $\mu$ ,  
defines BOTH  
the mean and  
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All observations  
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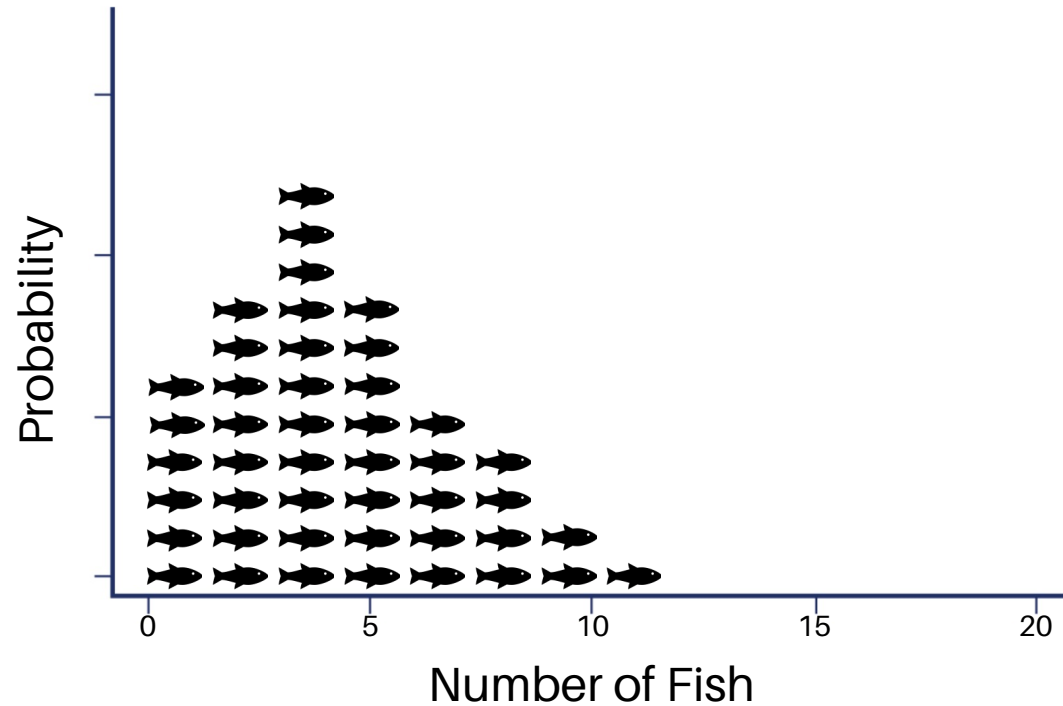
**Problems?**

# Problems?: Overdispersion

*When the variance is larger than the mean*

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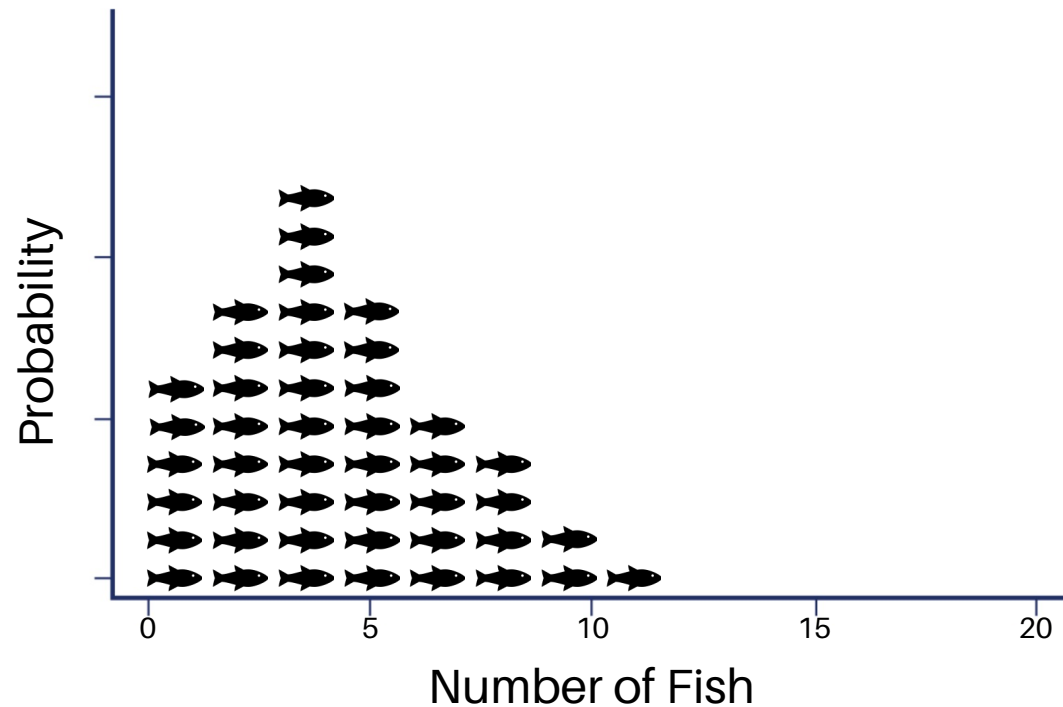
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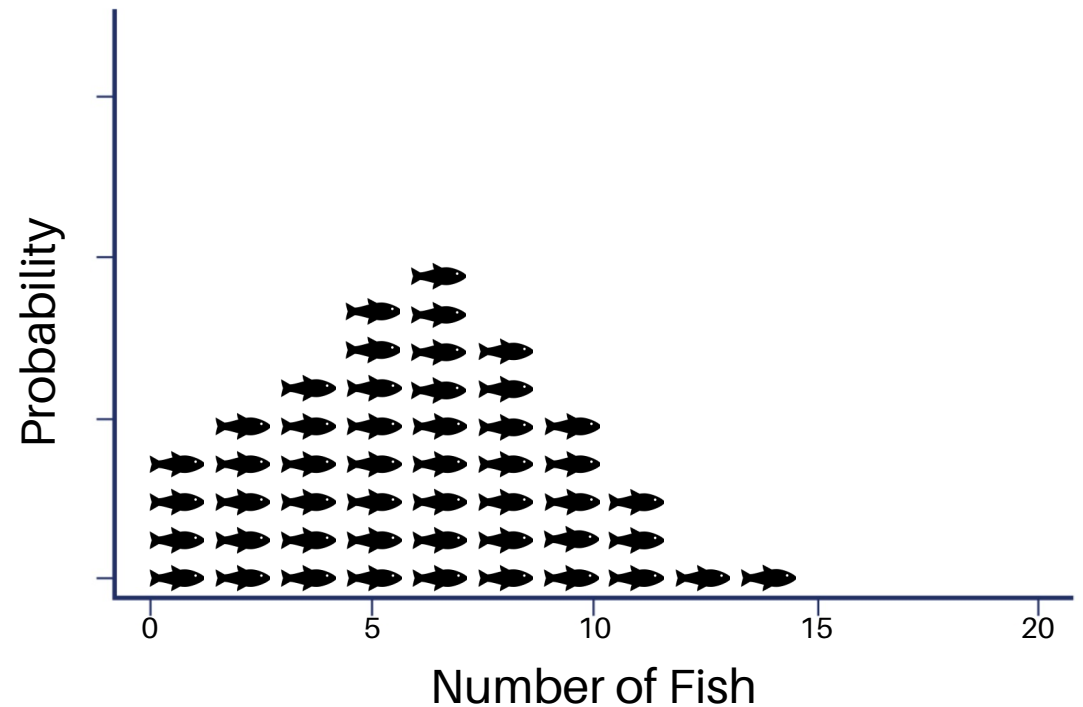
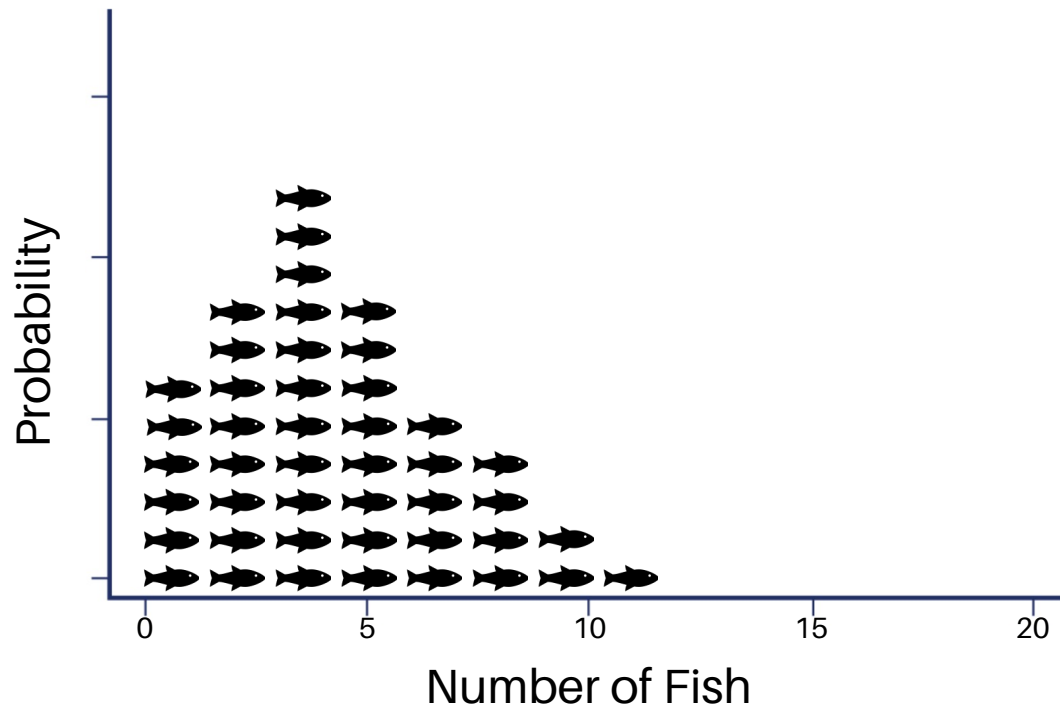
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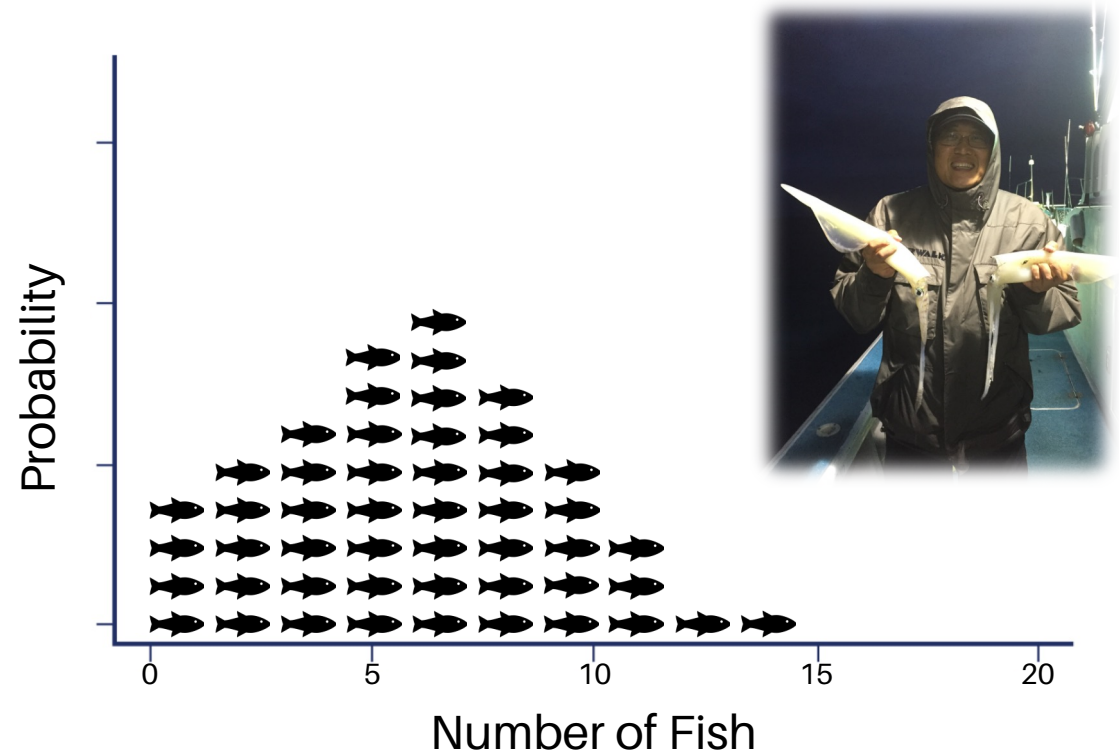
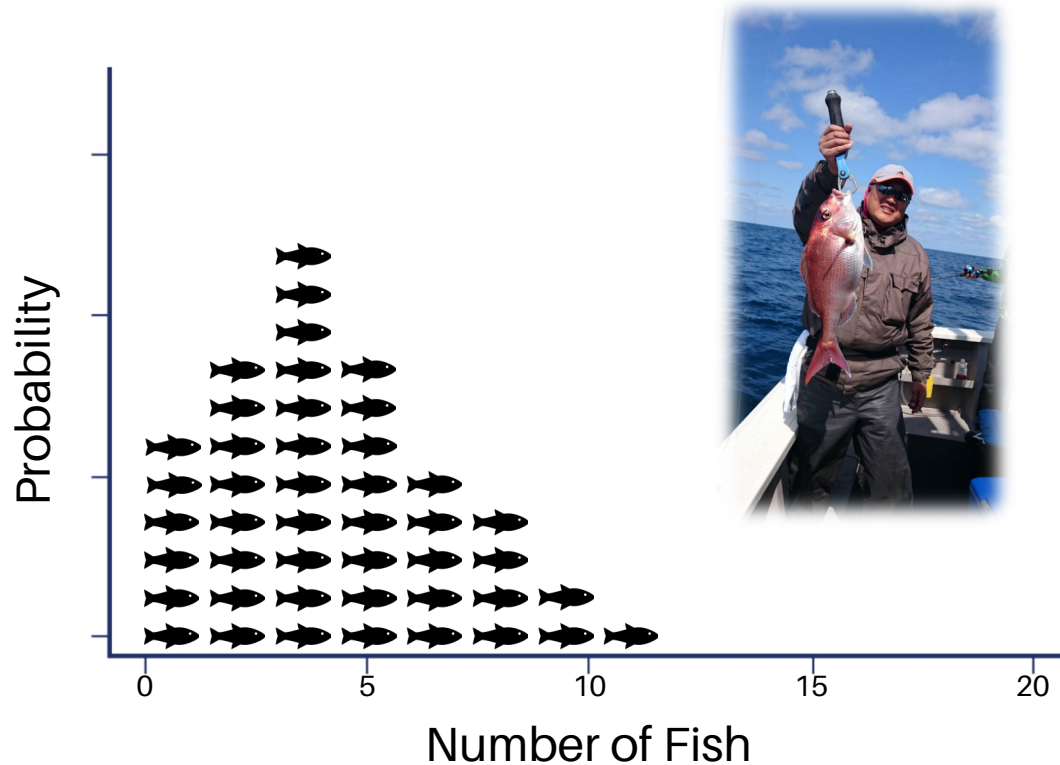
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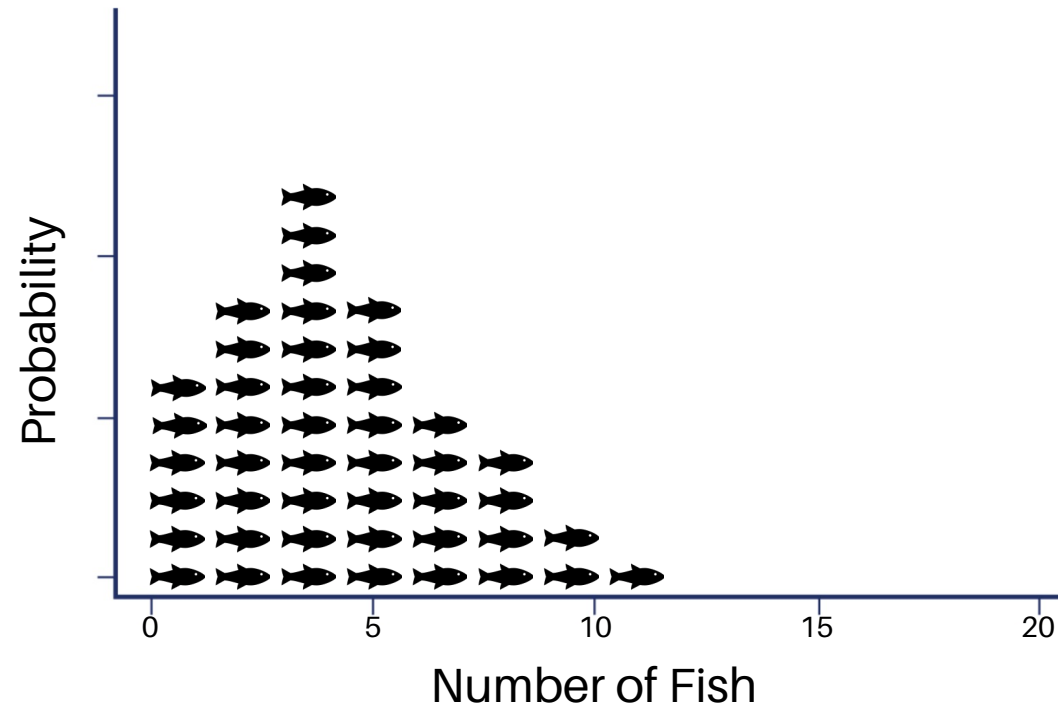
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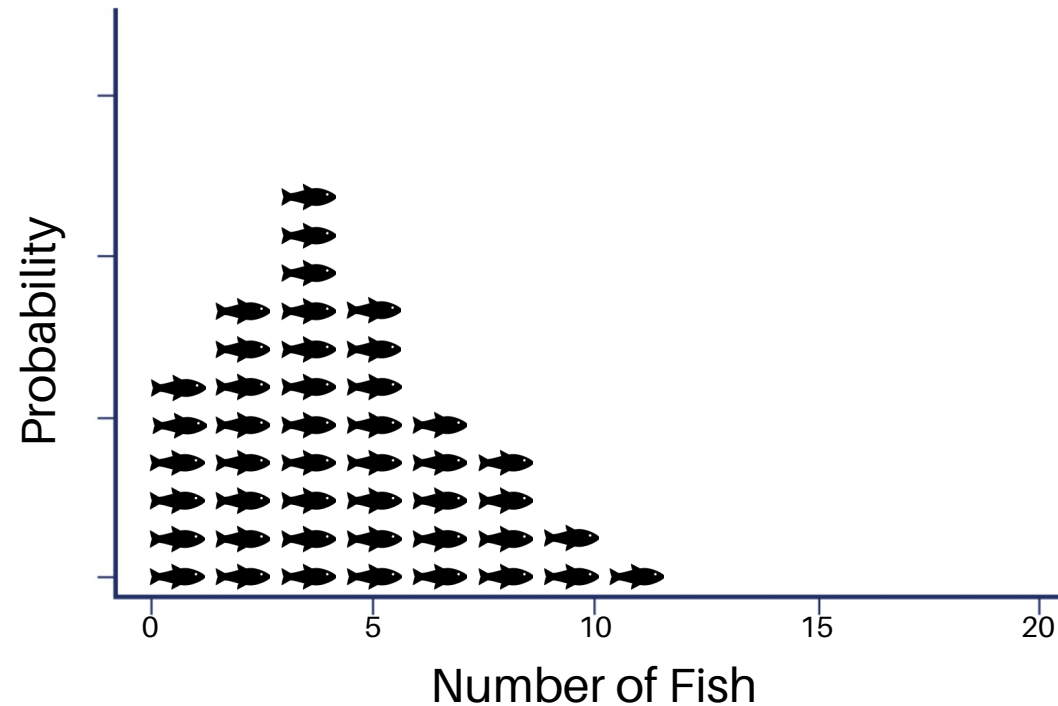
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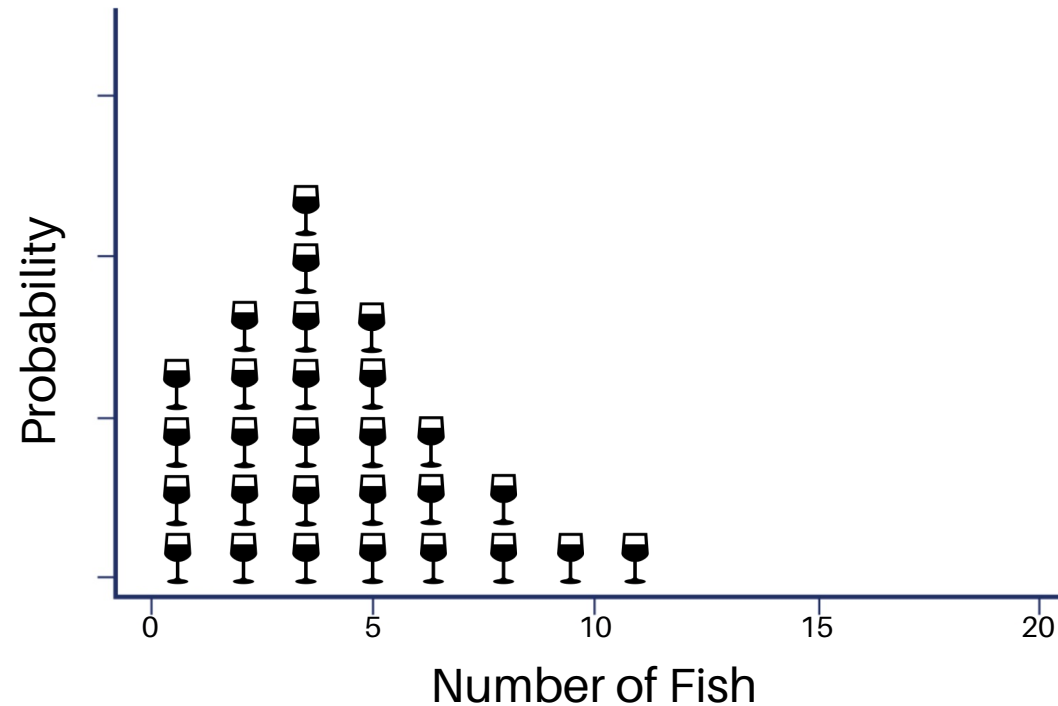
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- (1) Run an overdispersed model with a second parameter that defines the variance.
- (2) Run a negative binomial model instead, which assumes that there will be unexplained variability between individuals with the same predicted value.

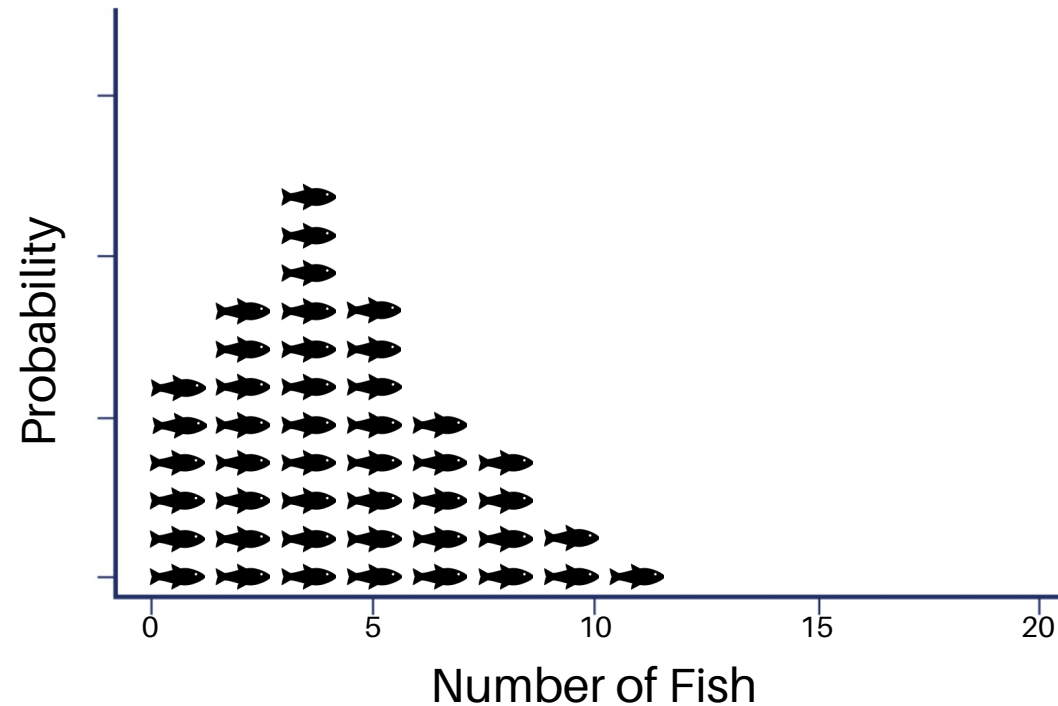
# Problems?: Zero inflated models

*When structural zeros artificially increase positive skew*



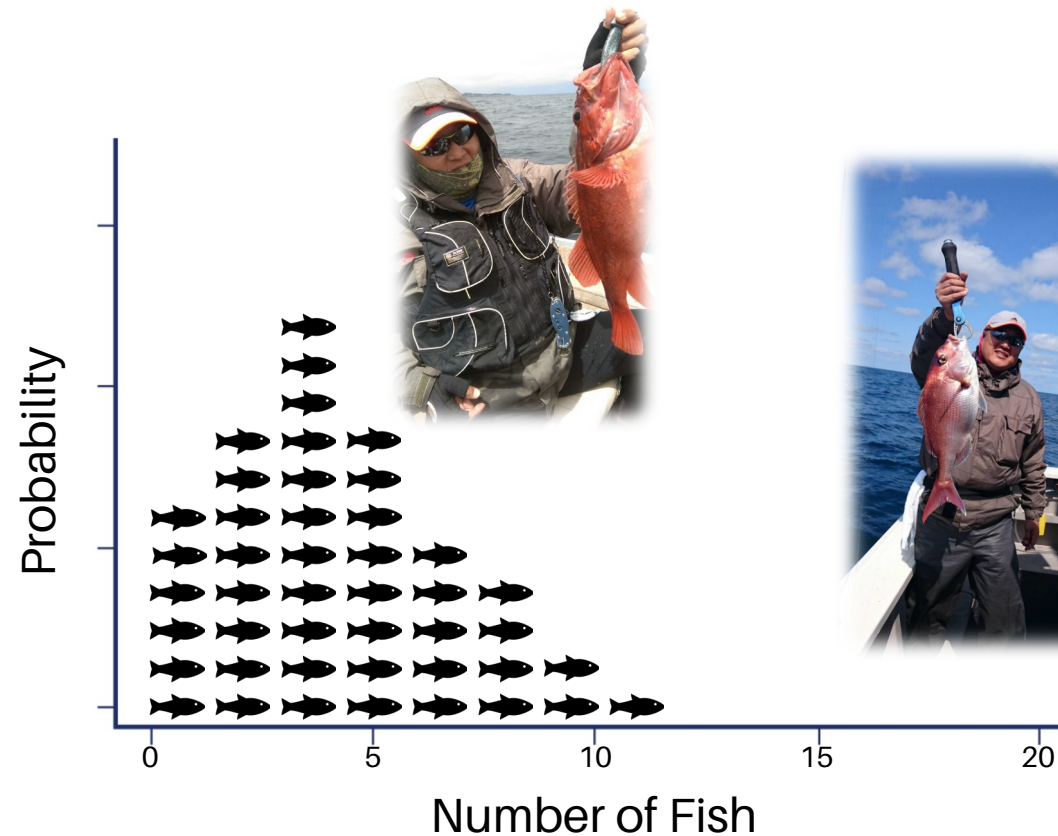
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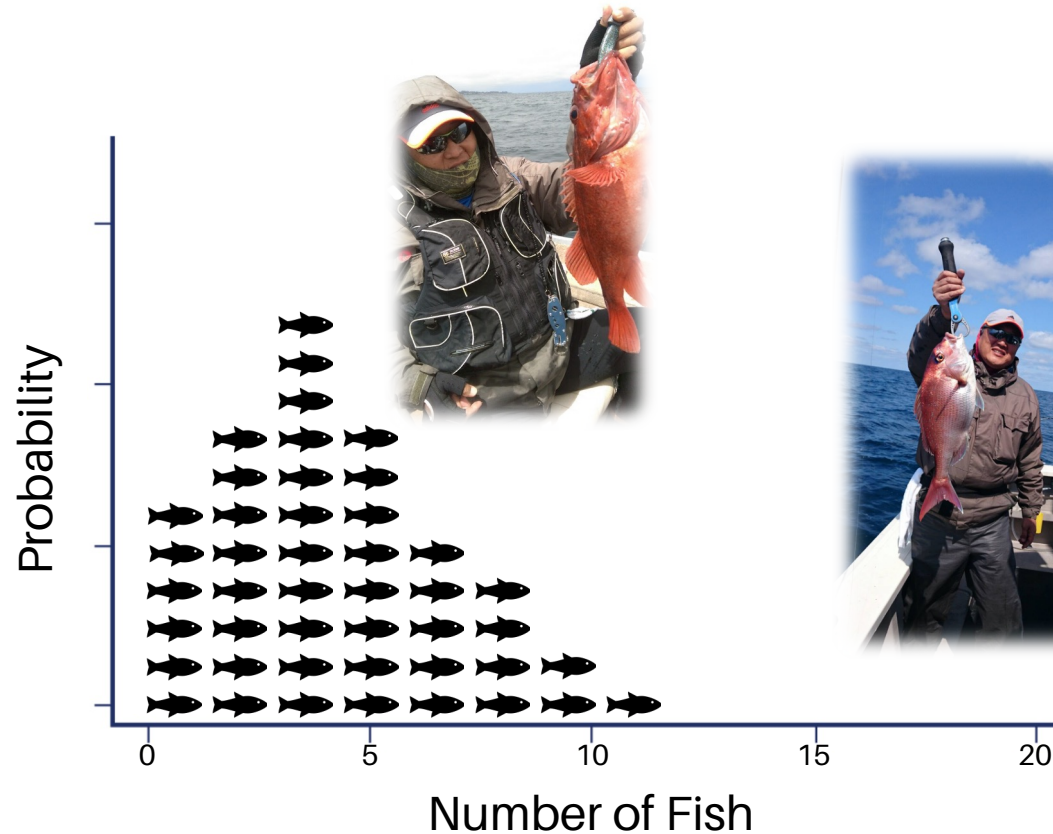
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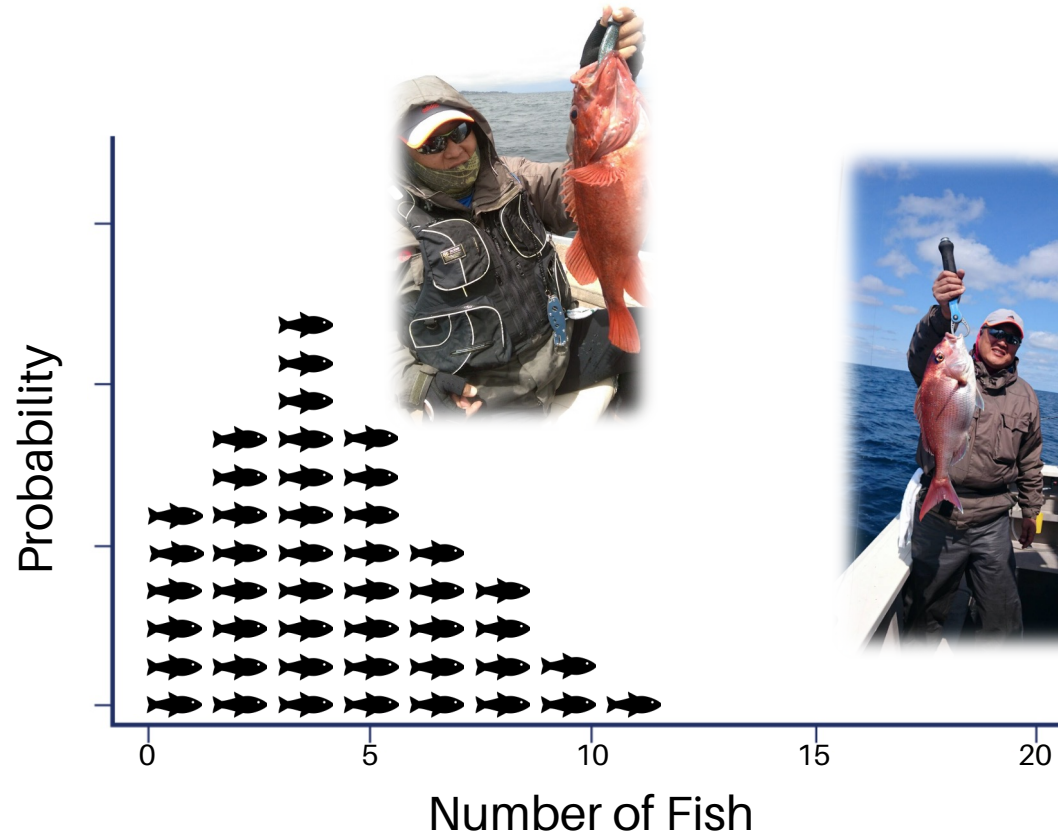
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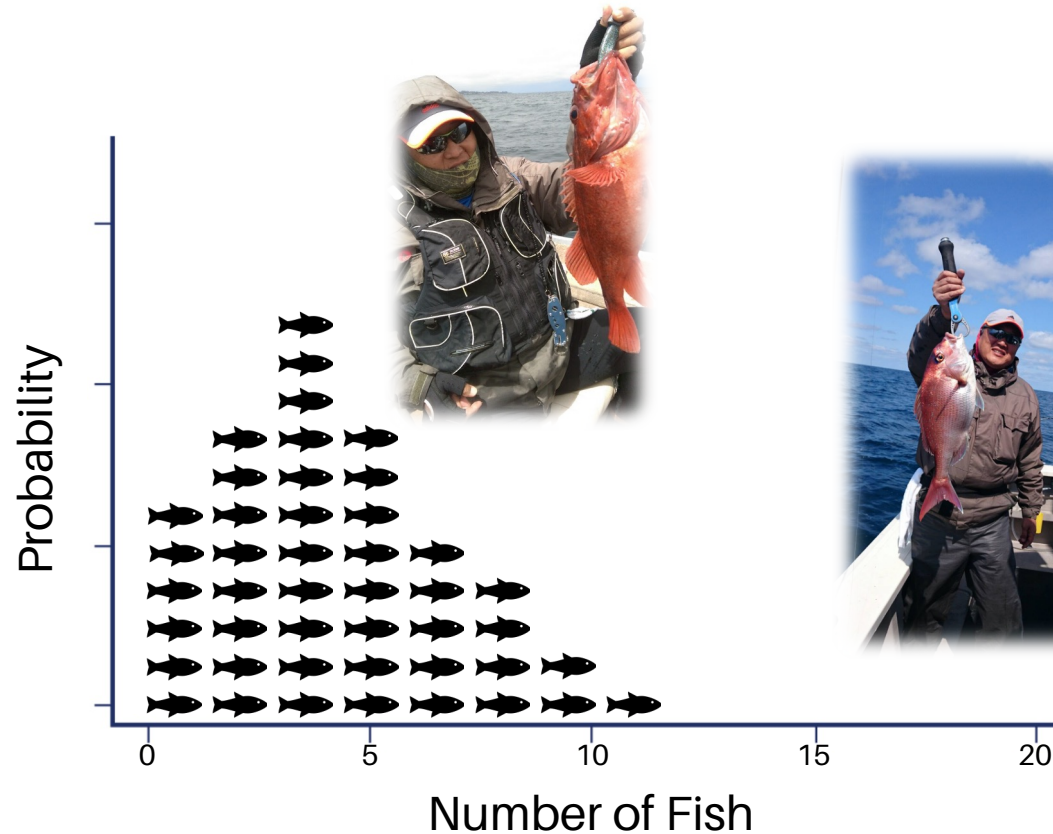
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*Best solution: Vet your sample beforehand*

# Other questions

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*In practice, is overdispersion ever not a problem? Why ever run a poisson regression over a negative binomial regression?*

*In reference to a previous conversation: To what extent are these concerns mitigated by taking a model comparison approach?*